

Inequalities Study Guide

Name: key

Identify the letter of the choice that best completes the statement or answer the question.

1. Write an inequality for the situation: *There are more than 19 cats in the shelter.*

1. $C > 19$

2. Write an inequality for the situation: *At least 50 pens are in the pencil-pouch.*

2. $P \geq 50$

3. What is the solution to the inequality $-2x - 40 > 8$?

$$\begin{aligned} -2x - 40 &> 8 \\ +40 &+40 \\ -2x &> 48 \\ \frac{-2x}{-2} &> \frac{48}{-2} \\ x &< -24 \end{aligned}$$

3. $X < -24$

★ 4. Which set of numbers is included in the solution set of $7 - 2x < -3$?

$$\begin{aligned} 7 - 2x &< -3 \\ -7 &-7 \\ -2x &< -10 \\ \frac{-2x}{-2} &< \frac{-10}{-2} \\ x &> 5 \end{aligned}$$

4. C

- a. {2.5, 8, 15} b. {-8, 0, 1.5} c. {15, 8, 5.5} d. {0, 2.5, 8}

Write the letters on the line of the numbers that are solutions to the inequalities.

5. $5y + 5 < 20$ a. 0

- b. 2 c. 5

5. a, b

$$\begin{aligned} 5y + 5 &< 20 \\ \frac{5y}{5} + \frac{5}{5} &< \frac{20}{5} \\ y + 1 &< 4 \\ y &< 3 \end{aligned}$$

6. $3p + 3 > -9$ a. 0

- b. -2 c. -4

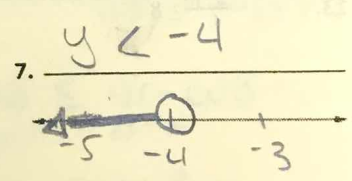
6. a, b

$$\begin{aligned} 3p + 3 &> -9 \\ \frac{3p}{3} + \frac{3}{3} &> \frac{-9}{3} \\ p + 1 &> -3 \\ p &> -4 \end{aligned}$$

Solve each inequality below and graph the solution set on the number line. Write your answer in the blank provided at the right.

★ 7. $-7v > 28$

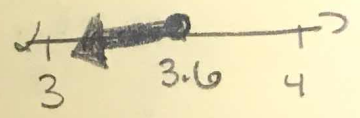
$$\begin{aligned} -7v &> 28 \\ \frac{-7v}{-7} &> \frac{28}{-7} \\ v &< -4 \end{aligned}$$



8. $3.5y + 5.7 \leq 18.2$

$$\begin{aligned} 3.5y + 5.7 &\leq 18.2 \\ \frac{3.5y}{3.5} + \frac{5.7}{3.5} &\leq \frac{18.2}{3.5} \\ 3.5y &\leq 12.5 \\ y &\leq 3.571... \\ y &\leq 3.6 \end{aligned}$$

8. $y \leq 3.6$



$$9. \quad \frac{z}{5} - 14 > -16$$

$$\quad \quad +14 \quad +14$$

$$(5) \frac{z}{5} > -2(5)$$

$$\boxed{z > -10}$$

$$\star 10. \quad -9w + 18 \geq -60$$

$$\quad \quad -18 \quad -18$$

$$\frac{-9w}{-9} \geq \frac{-78}{-9}$$

$$\boxed{w \leq 8\frac{2}{3}}$$

$$11. \quad 5(2x - 2) - 8x < -20$$

$$10x - 10 - 8x < -20$$

$$2x - 10 < -20$$

$$\quad +10 \quad +10$$

$$\frac{2x}{2} < \frac{-10}{2}$$

$$\boxed{x < -5}$$

$$12. \quad 6y + 3 - 5y \leq 8$$

$$y + 3 \leq 8$$

$$\quad -3 \quad -3$$

$$\boxed{y \leq 5}$$

$$\star 13. \quad (4) \frac{-8w - 10}{4} \geq 8(4)$$

$$-8w - 10 \geq 32$$

$$\quad +10 \quad +10$$

$$\frac{-8w}{-8} \geq \frac{42}{-8}$$

$$\boxed{w \leq -5\frac{1}{4}}$$

$$14. \quad 24 > 3(w + 7)$$

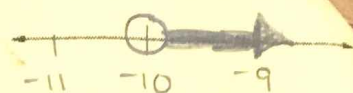
$$24 > 3w + 21$$

$$\quad -21 \quad -21$$

$$\frac{3}{3} > \frac{3w}{3}$$

$$1 > w$$

$$9. \quad z > -10$$



$$10. \quad w \leq 8\frac{2}{3}$$



$$11. \quad x < -5$$



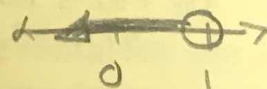
$$12. \quad y \leq 5$$



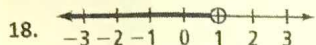
$$13. \quad w \leq -5\frac{1}{4}$$



$$14. \quad 1 > w$$



Write an inequality for each graph in the blank at the right.



18. $x < 1$

19. $x \geq -2$

20. Write an inequality that models the verbal expression and solve. Show your work.

One-half of a number increased by twenty is at most forty. Find the solution set.

Inequality: $\frac{1}{2}x + 20 \leq 40$

Work:

$$\begin{array}{r} \frac{1}{2}x + 20 \leq 40 \\ -20 \quad -20 \\ \hline \frac{1}{2}x \leq 20 \end{array}$$

$$x \leq 40$$

20. $x \leq 40$

For each problem below (1) Define a variable, (2) Write an inequality that models the situation, (3) Solve the inequality showing all work, and (4) Answer the question asked in the problem.

21. A local pizzeria offered a special of \$8.50 per pizza. A group of students spent less than \$65. They purchased three pitchers of soda for a total of \$10.99 and bought some pizzas. What is the maximum number of pizzas the group purchased?

Variable: p = # of pizzas

Inequality: $8.50p + 10.99 < 65$

$$\begin{array}{r} 8.50p + 10.99 < 65 \\ -10.99 \quad -10.99 \\ \hline 8.50p < 54.01 \\ \frac{8.50p}{8.50} < \frac{54.01}{8.50} \end{array}$$

Solution: $p < 6.4$

Maximum number of pizzas: 6 pizzas or less

22. The eighth grade wants to have their Promotion Ceremony at Time Warner Arena downtown. To rent the arena it costs \$2500 for the first two hours and \$550 for each additional hour. The students fundraised \$8530. What is the maximum amount of time the students can rent the Arena?

Variable: h = # of hours

Inequality: $2500 + 550(h-2) \leq 8530$

$$\begin{array}{r} 2500 + 550(h-2) \leq 8530 \\ 2500 + 550h - 1100 \leq 8530 \\ 1400 + 550h \leq 8530 \\ -1400 \quad -1400 \end{array}$$

$$\frac{550h}{550} \leq \frac{7130}{550}$$

$h \leq 12.9$

Solution: $h \leq 12.9$

Maximum amount of time: 12 hours

Bonus: Solve. $\frac{-3(4x-7)}{-2} > 5x - 2.2 + 17x$

$$\frac{-12x + 21}{-2} > 5x - 2.2 + 17x \quad (-2)$$

$$-12x + 21 < -2(22x - 2.2)$$

$$\begin{array}{r} -12x + 21 < -44x + 4.4 \\ +44x \quad +44x \end{array}$$

$$32x + 21 < 44$$

$$\begin{array}{r} 32x + 21 < 44 \\ -21 \quad -21 \end{array}$$

$$\begin{array}{r} 32x < 23 \\ \frac{32x}{32} < \frac{23}{32} \end{array}$$

$x < 0.5$